

## Appendix A. Model equations.

### State equations:

Carbon in vacuoles	$\dot{M}_{Cv} = F_{Cav} - h_g \times F_{Cm} - F_{Cg} - F_{Cvs}$	(A.1)
Carbon in structure	$\dot{M}_{Cs} = F_{Cvs} - (1 - h_g) \times F_{Cm}$	(A.2)

### C-fluxes:

Photosynthetic assimilation	$F_{Cav} = p\{I, C_{Ca}\} \times f\{M_{Cs}\} \times h_p\{C_{Cv}\}$	(A.3)
Growth	$F_{Cvs} = g\{T\} \times f\{M_{Cs}\} \times h_g\{C_{Cv}\}$	(A.4)
Maintenance respiration	$F_{Cm} = e\{T\} \times M_{Cs}$	(A.5)
Growth respiration	$F_{Cg} = \theta \times F_{Cvs}$	(A.6)

### Additional relations:

Carbon concentration in the vacuoles	$C_{Cv} = \frac{M_{Cv}}{\lambda \times M_{Cs}}$	(A.7)
Uninhibited photosynthesis rate	$p\{I, C_{Ca}\} = \frac{\varepsilon \times I \times \sigma \times (C_{Ca} - C_{C^*})}{\varepsilon \times I + \sigma \times (C_{Ca} - C_{C^*})} \quad C_{Ca} > C_{C^*}$	(A.8)
Photosynthesis inhibition function	$h_p\{C_{Cv}\} = \frac{1}{1 + \left( \frac{(1 - b_p) \times \Pi_v}{\Pi_v \times \gamma \times C_{Cv}} \right)^{s_p}}$	(A.9)
Source depletion switching (inhibition) function	$h_g\{C_{Cv}\} = \frac{1}{1 + \left( \frac{b_g \times \Pi_v}{\gamma \times C_{Cv}} \right)^{s_g}}$	(A.10)
Canopy closure reduction function	$f\{M_{Cs}\} = 1 - e^{-a \times M_{Cs}}$	(A.11)
Specific maintenance respiration	$e\{T\} = K \times e^{c \times (T - T^*)}$	(A.12)
Maximum growth rate	$g\{T\} = v \times e\{T\}$	(A.13)
*Osmotic pressure in vacuoles (Pa)	$\prod_v = P_v + \prod_r$	(A.14)
Nitrate concentration in the vacuoles	$C_{Nv} = \frac{\Pi_v - \gamma \times C_{Cv}}{\beta}$	(A.15)
The mols of nitrates per unit of dry weight	$C_{NO3N} = C_{Nv} \times \frac{V_v}{M_{DM}}$	(A.16)
The vacuolar volume	$V_v = \lambda \times M_{Cs}$	(A.17)

### Outputs:

#### Conversion between model states and experimental observations

Dry matter	$M_{DM} = \eta_{OMC} \times (M_{Cv} + M_{Cs}) + \eta_{MMN} \times \left( \frac{\lambda \times \prod_v}{\beta} \times M_{Cs} - \frac{\gamma}{\beta} M_{Cv} \right)$	(A.18)
Fresh matter	$M_{fm} = 1000 \times \lambda \times M_{Cs} + M_{DM}$	(A.19)
Nitrate content	$C_{NO3} = 10^6 \times \eta_{NO3N} \times C_{NO3N}$	(A.20)

## Appendix B. Parameter list.

### Initial conditions:

$M_{C_v}$	non-structural carbon content	0.007	$\text{mol}[\text{C}]\text{m}^{-2}[\text{ground}]$
$M_{C_s}$	structural carbon content	0.0671	$\text{mol}[\text{C}]\text{m}^{-2}[\text{ground}]$

### Input variables:

I	PAR inside the greenhouse	$\text{Wm}^{-2}$
$C_{Ca}$	CO2 concentration inside the greenhouse	ppm
T	air temperature	$^{\circ}\text{C}$

### Intermediate variables:

$F_{C_{av}}$	photosynthetic assimilation	$\text{mol}[\text{C}]\text{m}^{-2}[\text{ground}]\text{s}^{-1}$
$F_{C_{vs}}$	growth	$\text{mol}[\text{C}]\text{m}^{-2}[\text{ground}]\text{s}^{-1}$
$F_{C_m}$	maintenance respiration	$\text{mol}[\text{C}]\text{m}^{-2}[\text{ground}]\text{s}^{-1}$
$F_{C_g}$	growth respiration	$\text{mol}[\text{C}]\text{m}^{-2}[\text{ground}]\text{s}^{-1}$
$C_{Cv}$	carbon concentration in the vacuoles	$\text{mol}[\text{C}]\text{m}^{-3}$
$C_{Nv}$	nitrate concentration in the vacuoles	$\text{mol}[\text{N}]\text{m}^{-3}$
$C_{\text{NO}_3\text{N}}$	the mols of nitrates per unit of dry weight	$\text{mol}[\text{NO}_3]\text{kg}^{-1}[\text{m.s.}]$
$V_V$	the vacuolar volume	$\text{m}^3\text{m}^{-2}[\text{ground}]$

### Functions:

$p\{I, C_{Ca}\}$	uninhibited photosynthesis rate	$\text{mol}[\text{C}]\text{m}^{-2}[\text{ground}]\text{s}^{-1}$
$h_p\{C_{Cv}\}$	photosynthesis inhibition function	dimensionless
$h_g\{C_{Cv}\}$	source depletion switching (inhibition) function	dimensionless
$f\{M_{C_s}\}$	canopy closure reduction function	dimensionless
$e\{T\}$	specific maintenance respiration	$\text{s}^{-1}$
$g\{T\}$	maximum growth rate	$\text{mol}[\text{C}]\text{m}^{-2}[\text{ground}]\text{s}^{-1}$

### Output variables:

$M_{DM}$	dry matter	$\text{kg}[\text{m.s.}]\text{m}^{-2}[\text{ground}]$
$M_{fm}$	fresh matter	$\text{kg}[\text{m.s.}]\text{m}^{-2}[\text{ground}]$
$C_{\text{NO}_3}$	nitrate content	ppm

### Parameter values of the state equations:

#### Crop size

Leaf area closure parameter	a	0.2	$\text{m}^2[\text{ground}]\text{mol}^{-1}[\text{C}]$
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**Photosynthesis**

Apparent light use efficiency	$\varepsilon$	0.04-0.07	$\text{mol}[\text{C}]\text{mol}^{-1}[\text{PAP}]$
CO <sub>2</sub> transport coefficient	$\sigma$	$1.4\text{e}^{-3}$	$\text{ms}^{-1}$

**Respiration**

Maintenance respiration coefficient	k	$0.4\text{e}^{-6}$	$\text{s}^{-1}$
Temperature effect parameter	c	0.0693	$^{\circ}\text{C}^{-1}$
Growth respiration loss factor	$\theta$	0.3	dimensionless
Growth rate coefficient without inhibition from a closed canopy	v	22.1	$\text{mol}[\text{C}]\text{mol}^{-2}[\text{ground}]$

**Crop composition**

Coefficient of osmotic carbon equivalence	$\gamma$	0.61	$\text{m}^3\text{Pamol}^{-1}[\text{C}]$
Carbon concentration calculation parameter	$\lambda$	1/1200	$\text{m}^3\text{mol}^{-1}[\text{C}]$

**Attenuation**

Slope parameter of photosynthesis inhibition function	$h_p$	$s_p$	10	dimensionless
Slope parameter of growth inhibition function	$h_g$	$s_p$	10	dimensionless
Threshold parameter of photosynthesis inhibition function	$h_g$	$b_p$	0.8	dimensionless
Threshold parameter of growth inhibition function	$h_g$	$b_p$	0.2	dimensionless

**Values of constants of the model:**

CO <sub>2</sub> compensation point	$C_C^*$	0.0011	$\text{mol}[\text{C}]\text{mol}^{-3}$
Reference temperature	$T^*$	20	$^{\circ}\text{C}$
Osmotic pressure in the vacuoles	$\Pi_v$	580	Pa

**Additional parameter values of output equations:**

Regression parameter of C/N ratio in vacuoles	$\beta$	6.0	$\text{m}^3\text{Pamol}^{-1}[\text{N}]$
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**Values of constants of the output equations:**

Organic matter in kg per mol C	$\eta_{\text{OMC}}$	0.03	$\text{kg}[\text{DM}]\text{mol}^{-1}[\text{C}]$
Minerals in kg per mol N in vacuoles	$\eta_{\text{MMN}}$	0.148	$\text{kg}[\text{DM}]\text{mol}^{-1}[\text{N}]$
kg nitrate per mol N	$\eta_{\text{NO}_3\text{N}}$	0.062	$\text{kg}[\text{NO}_3]\text{mol}^{-1}[\text{N}]$