# INTERPRETACION DE PRUEBAS DE INYECCION EN YACIMIENTOS NATURALMENTE FRACTURADOS

# INTERPRETATION OF AFTER CLOSURE TESTS IN NATURALLY FRACTURED RESERVOIRS

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**RESUMEN:** Este estudio presenta un nuevo método para determinar la transmisibilidad en yacimientos naturalmente fracturados usando el análisis del flujo radial en pruebas de calibración. El método se basa en el análisis del comportamiento de la derivada de la presión con el tiempo. El objetivo es simplificar y facilitar la identificación del flujo radial y la "garganta" característica que se observa en la derivada cuando se tienen yacimientos naturalmente fracturados. El método propuesto no requiere el conocimiento previo de la presión de yacimiento. Un grafico logarítmico es usado para determinar la permeabilidad, la presión promedio, el almacenamiento y el coeficiente que relaciona las permeabilidades s de la matriz y de las fracturas en el yacimiento.

PALABRAS CLAVE: Yacimientos naturalmente fracturados, pruebas de flujo, TDS.

**ABSTRACT**: A new method for the determination of reservoir transmissibility using the after closure radial flow analysis of calibration tests was developed based on the pressure derivative. The primary objective of computing the pressure derivative with respect to the radial flow time function is to simplify and facilitate the identification of radial flow and the characteristic trough of a naturally fractured reservoir. The proposed method does not require a-priori the value of reservoir pressure. Only one log-log plot is used to determine the reservoir permeability, average pressure, storativity ratio, and interporosity flow coefficient.

The main conclusion of this study is that small mini-fracture treatments can be used as an effective tool to identify the presence of natural fractures and determine reservoir properties.

KEY WORDS: Naturally fractured reservoirs, Tiab's direct technique (TDS), after closure analysis, mini-frac.

# 1. INTRODUCCION

Using the theory of impulse testing and principle of superposition, Nolte et al [1] developed a method which allows the identification of radial flow and thus the determination of reservoir transmissibility and reservoir pressure. The exhibition of the radial flow is ensured by conducting a specialized calibration test called mini-fall off test. Benelkadi and Tiab [2] proposed a new procedure for determining reservoir permeability and the average reservoir pressure in homogeneous reservoirs. In this paper, the procedure is extended to naturally fractured reservoirs.

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# 2. INJECTION TEST AND NATURALLY FRACTURED RESERVOIRS

The mini-frac injection test has permitted the determination of the reservoir description in homogeneous reservoirs where fluid leakoff is dependent on the matrix permeability, fluid viscosity, and reservoir fluid compressibility. Applying this type of test to naturally fractured reservoirs introduces new factors that are difficult to measure, e.g. fluid leakoff dominated by the natural fractures that vary with stress or net pressure. This study allows the identification of naturally fractured reservoirs from after closure tests and the estimation of their respective reservoir parameters.

# 2.1 Naturally Fractured Reservoirs

Because of the complexity in the geometry of naturally fractured reservoirs, different mathematical approaches have been developed for diverse geometric shapes in an effort to simulate the effect of matrix block shapes in the transition period. One of the most popular approaches was proposed by Warren and Root [3]. They introduced two parameters that they referred to as the storativity ratio ( $\omega$ ) and the interporosity flow coefficient ( $\lambda$ ) to characterize naturally fractured reservoirs.

# 2.2 Injection Test

In the last two decades, mini fracture injection tests -also called calibration treatments or injection tests- have been developed to diagnose features including interpretation of near wellbore tortuosity and perforation friction, fracture height growth or confinement, pressuredependent leak-off, fracture closure, and more recently transmissibility and permeability.

Frequently, a calibration treatment is a test done right before the main stimulation treatment. This test follows a similar fracture treatment procedure but conducted, generally, without the addition of proppant, causing the fracture to have negligible conductivity when it closes. The short fracture created in this test allows the connection between the undamaged formation and the wellbore. Pressure analysis is based simultaneously on the principles of material balance, fracturing fluid flow, and rock elastic deformation (solid mechanics).

The calibration treatment sequence is shown in Figure 1, and consists of the following tests: mini fall off, step rate and mini-fracture test.



Figure 1. Calibration Treatment Sequence

# 2.1.1 Mini-falloff Test

The test is performed using inefficient fluids and a low injection rate. These characteristics make that the long term radial flow behavior that normally occurs only after a long shut-in period, can be attained during injection or shortly after closure in the mini-fall off test. This test allows the integration of information for analysis of preand after- closure analysis.

# 2.1.2 Step Rate Test

The step rate test is used to estimate fracture extension pressure and respective rates, thereby, determining the horsepower required to perform the fracture treatment.

# 2.1.3 Mini-fracture Test

Gathering the information obtained by the first two tests of the calibration treatment (a breakdown test may be also implemented into the treatment sequence), a mini-fracture test is performed. The determination of fracture propagation and fracture geometry during pumping is obtained by the implementation of Nolte-Smith [4] plot. This test is conducted with the fracturing fluid at the fracturing rate similar to the main fracturing treatment, but on a small scale. Figure 2 presents the fracturing evolution; each stage provides information for the fracture treatment design. This study is focused on the zone labeled as transient reservoir pressure near the wellbore.

In fact, natural fracture reservoirs enhanced fluid loss leading to a premature closing in the hydraulic fracture. In the cases that matrix permeability is high, the fluid leakoff process is not affected for the natural fractures; however, if matrix permeability is low the transmissibility of the natural fractures could be higher than the one from the matrix.



Figure 2. Example of fracturing-related pressure

### 2.3 Closure pressure and closure time

There are several methods in the literature for estimating closure pressure and closure time. Basically, this is the initial point for this study because the research is based on the pressure response after the fracture closes mechanically.

For the purposes of this study, the estimation of closure pressure and closure time follows the method presented by Jones et al [5]. They related the value of the fracture closure pressure to the minimum horizontal stress by the implementation of a derivative algorithm to identify different flow regimes.

The two relationships for an infinite conductivity fracture flow and finite conductivity fracture are, respectively:

$$\Delta P = A t^{0.5} \tag{1}$$

$$\Delta P = A' t^{0.25} \tag{2}$$

Where A and A' are grouping independents parameters, such as permeability, viscosity, and

compressibility, for infinite and finite conductivity fracture flow respectively.

Taking the logarithm on both sides of equations 1 and 2, and then differentiating them in respect to the logarithm of time:

 $\frac{d[\log(\Delta P)]}{d[\log(\Delta t)]} = 0.5 \quad \text{for infinite conductivity fracture}$ flow (3) And,

 $\frac{d[\log(\Delta P)]}{d[\log(\Delta t)]} = 0.25 \quad \text{for finite conductivity fracture}$ flow (4)

Then, a Cartesian plot of pressure derivative versus time would show a straight line of slope zero at a value of 0.5 for infinite conductivity, and 0.25 for finite conductivity. Jones et al [5] recommend to identify the closure pressure  $(P_c)$ at the pressure value corresponding to the end of the infinite conductivity fracture flow  $(t_e)$ . In case the infinite conductivity fracture flow is not observed, the recommendation is to read the value of pressure corresponding to the first point of the straight line of the finite conductivity fracture flow  $(t_s)$  as the value of closure pressure (see Figure 3 and Figure 4). The closure time can be obtained by adding the pumping time,  $t_p$ to  $t_e$  or  $t_s$ . The effect of skin will cause that the straight lines, representing the infinite and finite conductivity fracture flow, to not have the values of 0.5 and/or 0.25, respectively, in the derivative.



Figure 3. Example of estimation of closure pressure (P<sub>c</sub>) and ending time (t<sub>e</sub>) in presence of infinite conductivity fracture flow



Figure 4. Example of estimation of closure pressure (P<sub>c</sub>) and starting time (t<sub>s</sub>) in presence of finite conductivity fracture flow

#### 2.4 After-Closure Methods

The basis for After Closure Analysis (ACA) was initially proposed by Gu et al [6] and Abousleiman et al [7]. They demonstrated that properties of the injected fluid do not have any effect on the pressure response, acting like a skin effect because it is isolated to the near well area. Transient pressure response is dominant within the reservoir exhibiting linear or radial flow, losing its dependency from the mechanical response of an open fracture. This late time pressure falloff would be a good representation of the reservoir response allowing the estimation of reservoir pressure and permeability. The after closure response is similar to the behavior observed during conventional well test analysis, supporting an analogous methodology for its evaluation.

Nolte [8] introduced the concept of apparent time function. The after closure time function is selected to define various combinations of the reservoir parameters, including the estimation of closure time and reservoir pressure. The main assumptions of this dimensionless time function are the fracture closes instantaneously when pumping is stopped ( $t_c = t_p$ ) and significant spurt loss occurs. The concept of an apparent exposure time for the constant pressure period, as considered for a propagating fracture, is expressed as [8]:

$$F(t) = \sqrt{1 + \frac{t - t_c}{\chi t_c}} - \sqrt{\frac{t - t_c}{\chi t_c}}$$
(5)

The minimum value for time (t) in Equation 5 corresponds to the time that fracture closes  $(t_c)$ . This means that for  $t = t_c$  the value of the afterclosure dimensionless time function, F(t), is equal to the unity. Therefore, the maximum value achieved by the dimensionless time function is unity and its value decreases when real time increases. The term  $\chi t_c$  symbolizes an apparent time of closure, or equivalently, time of exposure to fluid loss and  $\chi \approx 1.62$ .

An excellent approximation for Equation 5 with an error percent less than 5% for  $t > 2.5t_c$  is given by [9]:

$$\frac{t_c}{t} = \left(\frac{\pi}{2}F\right)^2 \tag{6}$$

 $F^2$  approaches the equivalence of Horner behavior, achieving the time behavior of linear and radial flow from a single function. In fact, the mini-frac injection test is similar to the slug test or the impulse test.

Then, the instantaneous source solution is applied to the diffusivity equation in order to model the pressure response of the reservoir. This concept implies a sudden extraction or release of fluid at the source in the reservoir creating a pressure change throughout the system. The sources are distributed until the fracture closes and there is no more leakoff into the formation. Abousleiman et al [7] define the after closure pressure response as a result of instantaneous point source solution by applying Duhamel's principle of superposition for time  $t \ge t_c$ :

$$P(x, y, t) = \int_{-Lm}^{Lm} \xi_d(x') \int_{\xi_d(x')}^{\xi_d(x')} q_l(x', t') \Delta P_f dt' dx'$$
(7)

#### **3. MATHEMATICAL MODEL**

Conventional pressure transient tests in low permeability reservoirs require a long duration to observe all flow regimes necessary for determining correctly all reservoir and nearwellbore parameters. The cost of these tests is

generally very high because of additional equipment and production. Short-time tests, such as drill stem test and impulse test, provide local estimations of the properties in the reservoir that are usually contaminated by nearwellbore damage. Alternatively, the calibration test, as discussed previously, follows a procedure similar to the hydraulic fracturing treatment but only a small fracture is induced in the formation to overcome formation damage. The pressure response during a calibration test is estimated by the instantaneous line source solution of the diffusivity equation. The mathematical approach discussed in this section is specifically for the calibration test. The following assumptions are made: 1) the fracture and matrix are distributed homogeneously throughout the formation, 2) reservoir is fractured by a fluid injection and this created fracture has a constant height equal to the reservoir height, 3) the fluid injection has the same property as the reservoir fluid, 4) the fracture created is a Perkins-Kern-Nordgren type (PKN) [9], [10], 5) closed fracture is of zero conductivity (hydraulically and mechanically) and 6)natural fractures do not close.

Following a procedure similar to the one Benelkadi and Tiab [2] proposed for conventional reservoirs, the response of pressure difference and pressure derivative versus an apparent function of time for naturally fractured reservoirs is expected to show a trend similar to the one in conventional techniques.  $F^2$  is a time function similar to Horner time; therefore, late times correspond to low values of  $F^2$ , and early times to values of  $F^2$  close to unity. The maximum value of  $F^2$  is unity, which corresponds to the value of closure time. Therefore, the expected shape obtained by this method is shown in Figure 3.

Similarly to the *TDS* (*Tiab's Direct Synthesis*) technique in naturally fractured reservoirs, it is possible to identify unique characteristic points from Figure 5 for calculating various reservoir parameters. The nomenclature for these points is:

$(\mathbf{F}^2 \times \Delta \mathbf{P'})_{\mathbf{R}}$	radial flow, psi
$F_1^2$	beginning of the trough
$F_2^2$	base of the trough
$F_{3}^{2}$	end of the trough



Figure 5. Idealized sketch of the characteristic points detected on a logarithmic plot of pressure and pressure derivative versus F<sup>2</sup>

# **3.1** Intermediate time– appreciation of the trough F<sup>2</sup> Procedure

Analogous to the *TDS* technique, the plot of pressure and pressure derivative versus  $F^2$  shows a *trough* at intermediate times. Previous investigations [11], [12] have proven that a logarithmic plot of pressure derivative versus dimensionless time allows the identification of characteristic points for calculating storativity ratio and interporosity coefficient at the

$$\left[t_D\right]_1 = 0.01 \frac{\omega(1-\omega)}{\lambda} \tag{8}$$

$$[t_D]_2 = \frac{\omega}{\lambda} \ln\left(\frac{1}{\omega}\right) \tag{9}$$

$$[t_D]_3 = \frac{4}{\lambda} \tag{10}$$

Defining dimensionless time as:

$$t_D = 4 \times 10^{-6} \frac{kt}{\phi \mu c_t r_w^2}$$
(11)

After mathematical manipulation of Nolte's apparent time function approximation (i.e. Eq. 6) and combining it with dimensionless time (i.e. Eq. 11) in function of  $F^2$  the following equations are obtained at the beginning, base, and end of the trough, respectively:

$$\omega(1-\omega) = 4 \times 10^2 \frac{F_3^2}{F_1^2}$$
(12)

$$\omega^{\omega} = EXP\left(-4 \times \frac{F_3^2}{F_2^2}\right) \tag{13}$$

$$\lambda = 2.5 \times 10^6 \left(\frac{\phi \mu c_l r_w^2}{k t_c}\right) F_3^2 \tag{14}$$

In order to calculate  $\omega$  by Equation 12 we must first determine the value of the right side of the equation; then read the value of the corresponding  $\omega$  from Figure 6 (for  $\omega < 50\%$ ). The following correlation is obtained from Figure 6:

$$\omega = \frac{1.3834A - 0.0064}{1 + 3.3554A - 17.2951A^2}$$
(15)  
Where A =  $\omega(1 - \omega) = 400(F_3^2/F_1^2)$ .

It is important to notice that this correlation implies  $0 \le \omega \le 0.45$  and  $0 \le A \le 0.25$ . Furthermore, Figure 6 shows that the value of  $\omega(1-\omega)$  varies between 0 and 0.25. This range allows the estimation of  $\omega$  from reading the values of  $F_1^2$  and  $F_3^2$  and the quadratic solution of Equation 12 without obtaining imaginary results. Substituting for *A* into Eq. 15 yields:

$$\omega = \frac{553.36 \left(\frac{F_3^2}{F_1^2}\right) - 0.0064}{1 + 1342.16 \left(\frac{F_3^2}{F_1^2}\right) - 2767216 \left(\frac{F_3^2}{F_1^2}\right)^2}$$
(15a)



**Figure 6.** Graphical representation of  $\omega$  versus  $\omega(1-\omega)$ 

From Figure 6 only the negative solution of the quadratic solution is applicable (values of storativity in the range of  $0 < \omega < 0.5$ ); therefore  $\omega$  can also be calculated from the following equation:

$$\omega = \frac{1 - \sqrt{1 - 4A}}{2} = 0.5 \left( 1 - \sqrt{1 - 1600 \left(\frac{F_3^2}{F_1^2}\right)} \right) \quad (16)$$

To calculate  $\omega$  by Equation 13 it is required to determine the value of the right side of the equation; then read the value of the corresponding  $\omega$  from Figure 7 (for  $\omega < 35\%$ ). The following correlation is obtained from Figure 7:

$$\omega = \frac{0.118B - 0.106}{1 + 0.517B - 0.750B^2} \tag{17}$$

Where  $B = (1/\omega)^{\omega}$ . Note that this correlation implies  $0 \le \omega \le 0.35$  and  $1 \le B \le 1.44$ .

### **3.2** Late Time - Radial Flow F<sup>2</sup> Procedure

The instantaneous line source solution for naturally fractured reservoirs presented by Chipperfield [13] is used to evaluate the double integral in Equation 7. At late times  $t_1$  behaves as  $t_1(x') \approx \Delta t$ , and  $t_1 - t' \approx \Delta t$ , so Equation 7 becomes:

$$P(\Delta t) = \frac{\mu}{4\pi k_f} \int_{-Lm}^{Lm} \int_{0}^{\xi_o(x')} q_I(t') \left(\frac{1}{\Delta t} - \frac{\eta_f S_m}{\tau} e^{-\frac{\Delta t}{\tau}}\right) e^{-\frac{r^2}{4\eta_f \Delta t}} dt' dx'$$
(18)



**Figure 7.** Graphical representation of  $\omega$  versus  $(1/\omega)^{\omega}$ 

Where *m* stands for matrix and *f* for fractures. *S* is the storativity  $(\omega \mu c_t)$ , T<sub>f</sub> is transmissibility for the fractures and  $\eta_f$  the diffusivity as a function of time [13].

During radial flow (late time)  $\Delta t$  is independent of x' and t' then Equation 18 becomes:

$$P(\Delta t) = \frac{\mu}{4\pi k_f \Delta t} \int_{-Lm}^{Lm} \int_{0}^{\xi_o(x')} q_I(t') dt' dx'$$
(19)

Applying the solution presented by Abousleiman et al. [9] for the double integral of Equation 19 we have:

$$P(\Delta t) = \frac{\mu}{4\pi k \Delta t} \times \frac{Q_o t_p}{h}$$
(20)

The injected fluid volume  $V_i$  is defined as the product of the average injection rate and closure time [7], then:

$$P(\Delta t) = \frac{V_i \mu}{4\pi kh} \times \frac{1}{\Delta t}$$
(21)

Multiplying and dividing Equation 21 by  $t_c$  and combining it with the concept of apparent closure time (i.e. Equation 6):

$$\Delta P = 2.5 \times 10^5 \frac{V_i \mu}{k h t_c} F^2 \tag{22}$$

The derivative of Equation 22 with respect to  $F^2$  is:

$$\frac{d\Delta P}{d(F^2)} = 2.5 \times 10^5 \frac{V_i \mu}{kht_c}$$
(23)

Then, during radial flow a plot of  $\Delta P$  versus  $F^2$  on a log-log graph is a straight line of a slope of unity and the derivative has a slope equal to zero. The permeability is calculated by extrapolating this horizontal straight line until it intercepts the y axis, similarly to the *TDS* technique:

$$k = 2.5 \times 10^5 \frac{V_i \mu}{h t_c (F^2 \times \Delta P')_R}$$
(24)

On the log-log plot the pressure and pressure derivative have the same value when  $F^2$  is equal to the unity. Then, the unit slope line must intercept the horizontal line at  $F^2 = 1$  at the value of  $(F^2 \times \Delta P')_R$ . In other words, combining the equations for pressure derivative and pressure difference it is possible to determine that the straight line, which corresponds to the radial flow in the pressure difference, has a slope equal to unity and its intercept corresponds to the value of  $(F^2 \times \Delta P')_R$ . The equation of this straight line is:

$$\overline{P} = \left(P_w\right)_R - F_R^2 \left(F^2 \times \Delta P'\right)_R \tag{25}$$

Where  $(P_w)_R$  is the value of  $P_w$  that corresponds to  $F^2$  read at any point on the radial flow portion.

Pressure derivative [2], [14] is more sensitive to time change than the pressure function and is not affected by the value of the reservoir pressure. Then, if the bottomhole pressure curve is incorporated to the diagnostic plot and the derivative is estimated in function of P<sub>w</sub> instead of  $\Delta P$ , the average reservoir pressure can be calculated using Equation 25. This means, Equation 25 allows for the calculation of average reservoir pressure without the need of guessing reservoir pressures as it was required before. For verification of average reservoir pressure, the radial flow portion of the pressure difference plot must lay on a unit slope crossing  $F^2$  at the value of 1 and  $(F^2 \times P'_w)_R$ .

#### 3.3 Special Cases

3.3.1 Comparison of  $\omega$  with the one obtained by the TDS technique at the minimum point of the trough

Tiab and Donalson [14] obtained the following relationship at the minimum point of the trough:

$$\omega = \left(2.9114 - \frac{3.5688}{\ln(N_s)} - \frac{6.5452}{N_s}\right)^{-1}$$
(26)

Where,

$$N_s = EXP(-\lambda t_{D\min}) \tag{27}$$

$$t_{D\min} = \left(\frac{0.0002637k}{\mu r_w^2 (\phi c_t)_{m+f}}\right) t_{\min}$$
(28)

 $t_{min}$  (in hours) is the time coordinate of the minimum point of the trough on the pressure derivative curve.

Combining Equations 13 and 27 gives:

$$N_s = EXP\left(-4 \times \frac{F_3^2}{F_2^2}\right) \tag{29}$$

Combining Equations 29 and 26 yields:

$$\omega = \left(2.9114 + 0.8922 \frac{F_2^2}{F_3^2} - 6.5452 e^{\left(4 \times \frac{F_3^2}{F_2^2}\right)}\right)^{-1}$$
(30)

# 3.3.2 The beginning and base of the trough are difficult to observe

Engler and Tiab [15] developed the following equation for the intersection point of the infinite acting line and the unit slope of the transition period:

$$\lambda = \frac{1}{t_{Dx}} \tag{31}$$

Where x stands for the intersection point and time is expressed in hours. Combining Equation 31 with Equations 11 and 6, the intersection point of the unit slope line at intermediate times and the radial flow line gives:

$$\lambda = 616850 \left( \frac{\phi \mu c_i r_w^2}{k t_c} \right) F_x^2$$
(32)

Another useful equation developed by Engler and Tiab [15] relates the value of  $\lambda$  and  $\omega$  at the beginning of the radial flow:

$$\lambda = \frac{5(1-\omega)}{t_{D3}} \tag{33}$$

The combination of Equations 33, 11, and 6 gives:

$$\omega = 1 - 3.6 \times 10^{-7} \frac{\lambda \, kt_c}{\phi \mu c_t r_w^2 F_3^2} \tag{34}$$

#### 3.4 Step-by-step procedure

The following step by step procedure is recommended for the determination of permeability (k), average reservoir pressure (P<sub>r</sub>), storativity ratio ( $\omega$ ), and interporosity flow coefficient ( $\lambda$ ).

*Step 1* - Following a mini-falloff test, acquire, compute and prepare the following required input parameters:

• Pressure and time data pertinent to both the injection and the fall off periods of the test.

- Injection flow rate q, and the total volume of the fluid injected into the fracture, V<sub>i</sub>.
- Reservoir fluid viscosity, μ; fracture height, h; Pumping time, t<sub>p</sub>; wellbore radius, r<sub>w</sub>; and formation compressibility, c<sub>t</sub>.

Step 2 - Convert the time data into shut in time intervals (i.e.  $\Delta t$ ).

*Step 3* - Identify and determine the closure pressure and the closure time. The method applied here for calculating closure pressure and closure time is referred to the one developed by Jones and Sargeant [5]

Step 4 - Compute the radial flow time function  $F^2$ :

$$F^{2} = \left(\sqrt{1 + \frac{t - t_{c}}{\chi t_{c}}} - \sqrt{\frac{t - t_{c}}{\chi t_{c}}}\right)^{2}$$
(35)

*Step 5* - Compute the pressure derivative with respect to the dimensionless time function with the following equation:

$$\left(\frac{\partial P}{\partial F^2}\right)_i = \frac{\left[\frac{\left(P_i - P_{i-1}\right)\left(F_{i+1}^2 - F_i^2\right)}{F_i^2 - F_{i-1}^2} + \frac{\left(P_{i+1} - P_i\right)\left(F_i^2 - F_{i-1}^2\right)}{F_{i+1}^2 - F_i^2}\right]}{\left(F_{i+1}^2 - F_{i-1}^2\right)}$$
(36)

*Step 6* - Plot the bottomhole pressure and its derivative on the same log-log plot.

*Step 7* - Identify radial flow and calculate reservoir pressure with Equation 25.

Step 8 - With the estimated reservoir pressure, calculate pressure difference and plot it in the same logarithmic plot with the pressure derivative and bottomhole pressure. Verify the value of reservoir pressure tracing a straight line of unit slope crossing  $F^2 = 1$ ; radial flow must overlay on this straight line.

Step 9 - The derivative curve would show a trough at intermediate times. This is a characteristic of a naturally fractured reservoir. Read the values of  $F_{1}^{2}$ ,  $F_{2}^{2}$ ,  $F_{3}^{2}$ , and  $F_{x}^{2}$  at the beginning, base, end of the trough, and intersection point between unit slope at intermediate times and radial flow respectively. These characteristic points correspond to the

inflection points in the pressure difference curve and, because of noise, can be read more accurately from the pressure difference curve (Figure 5).

*Step 10* - Estimate the formation permeability, k, from the infinite acting radial flow line on the pressure derivative curve using Equation 24.

*Step 11* - Calculate the interporosity flow coefficient by Equations 14 and/or 32. In the case that more than one equation could be applied to the analysis, use them for verification purposes as well as for a better setting of characteristic points.

*Step 12* - Calculate the storativity ratio with:

- Equation 12 and Figure 6, Equation 15, and/or Equation 16 for the beginning of the trough;
- Equation 13 and Figure 7, Equation 17, Equation 26, and/or Equation 30 for the base of the trough; and
- Equation 34 for the end of the trough.

In the case that more than one equation could be applied to the analysis, use them for verification purposes as well as for a better setting of characteristic points.

#### 4. FIELD EXAMPLE

This example is taken from Benelkadi and Tiab [2]. This is a calibration test applied to an oil well from TFT field (Algeria). The purpose of this job is to collect information about leak-off characteristics of the fracturing fluid. Determination of the fracture dimensions (fracture half length and average fracture width) and estimation of the fracture geometry model is also accomplished by means of interpretation and analysis from mini-fracture test. The test was performed by pumping 5000 gallons (119 bbl) of linear gel at an approximate rate of 13 bbl/min (pumping time was 9.1 min). The bottomhole pressure decline was monitored for 57 minutes.

Other parameters are:

$\phi = 9.00 \%$	$\mu = 0.355 \text{ cp}$	h = 32.8
$V_i = 119 \text{ bbl}$	$t_p = 9.1 \text{ min}$	$r_{w} = 0.25$
ft $c_t = 7.112 \times 10^{-5} \text{ psi}^{-1}$		

Step-by-step procedure:

Steps 1 and 2 - The information pertinent to these steps is reported above.

Step 3 – Determine closure pressure and closure time.

Following the procedure suggested by Jones and Sargeant [5], Figure 8 permits the identification of  $P_c = 3208.76$  psi and  $t_s = 1.23$  min then  $t_c = 1.23+9.1=10.33$  min. These values are close to the ones reported by Benelkadi and Tiab [2],  $P_c = 3210$  psi and  $t_c = 10.43$  min.

Step 4 and 5 - Compute  $F^2$  and  $F^2 \times P_w'$ .

Step 6 - Plot bottomhole pressure and its derivative on the same logarithmic plot as shown in Figure 9. From this Figure the following data can be read:

$$(F^2 \times P_w')_R = 2550 \text{ psi}$$
  $(F^2)_R = 0.066543$   
 $(P_w)_R = 2511.81 \text{ psi}$ 



Figure 8. Plot for estimating closure pressure and closure time, Field example



Figure 9. Pressure and pressure derivative plot, Field example

Step 7 - Identify radial flow and calculate average reservoir pressure with Equation 25.

 $\overline{P} = 2511.81 - (0.0666543)(2550) = 2341.84 \text{ psi}$ 

Step 8 - With the estimated average reservoir pressure, calculate pressure difference and plot it in the same logarithmic plot. Verify the value of reservoir pressure.

Step 9 - Read the values of  $F_{1}^{2}$ ,  $F_{2}^{2}$ , and  $F_{3}^{2}$ .

Despite the fact that it is possible to identify the inflection point in the pressure difference curve, the behavior on the derivative shows wellbore storage effects.

From Figure 10 read:

$$F_3^2 = 0.096$$
  $F_x^2 = 0.11$ 



Figure 10. Diagnostic plot, Field example

Step 10 – Use Eq. 24 to calculate the formation permeability:

$$k = 2.5 \times 10^5 \frac{(119)(0.355)}{(32.8)(10.33)(2550)} = 12.22$$
 ma

Step 11 - Calculate the interporosity flow coefficient:

*Calculation of*  $\lambda$  *with Equation 14:* 

 $\lambda = 2.5 \times 10^{6} \frac{(0.09)(0.355)(7.112 \times 10^{-5})(0.25)^{2}(0.096)}{(12.22)(10.33)} = 2.70 \times 10^{-4}$ 

Step 12 - Calculate the storativity ratio.

Calculation of  $\omega$  with Equation 34:

$$\omega = 1 - 3.6 \times 10^{-7} \frac{(2.70 \times 10^{-4})(12.22)(10.33)}{(0.09)(0.355)(7.112 \times 10^{-5})(0.25)^2(0.096)} = 0.100$$

Table 1 summarizes the estimated values of  $\omega$ ,  $\lambda$ ,  $P_r$ , and k for the field Example. It is important to notice that both methods complement each other, allowing a robust methodology for the interpretation of the naturally fractured reservoir from a mini-falloff data.

 Table 1. Summary of Results

Example	$\overline{P}$ , psi	k, md	ω	λ
Benelkadi and Tiab [2]	2350	12.4	-	-
F <sup>2</sup> Procedure	2342	12.22	0.1	2.70×10 <sup>-4</sup>

#### 5. CONCLUSIONS

1. Mini-fracture treatment can be used as an effective tool to identify the presence of natural fractures and determine reservoir properties, such as permeability, storativity ratio, interporosity, and average reservoir pressure.

2. The average reservoir pressure can be calculated from the proposed technique. It is calculated from characteristic points in the diagnostic plot in an accurate and straightforward procedure.

3. A set of alternative equations for estimating permeability, storativity and interporosity for

special cases is presented. The combination of all the equations that have been presented here permits a complete analysis of the system, using equations for verification purposes and for identification of the different flow regimes and characteristic points.

4. The technique presented is analogous to the *Tiab's Direct Synthesis* technique. From a single log-log plot it is possible to identify characteristic points in order to estimate reservoir properties.

5. The main limitation of this technique is that in the absence of a trough, due to wellbore storage effects, it is not possible to estimate  $\lambda$  and  $\omega$ .

# 6. NOMENCLATURE

- A dummy variable
- B dummy variable
- b dummy variable
- F(t) time function, dimensionless

 $F^2 \times \Delta P$  pressure derivative respect time function F2

- g gravity
- h formation thickness, ft
- k permeability, md

P, p Pressure, psi

- $q_l(x,t)$  leakoff intensity
- $\hat{Q}_{o}$  injected rate, bbl/min
- r<sub>w</sub> wellbore radius, ft
- t time, min
- t<sub>c</sub> closure time, min
- t<sub>p</sub> pumping time, min
- t' leakoff exposure time of the fracture element, min
- v velocity
- V ratio of the total volume of the medium to the bulk volume of the system, ft3

Greek Symbols

- $\phi$  porosity, fraction
- η dummy variable
- ρ density
- $\rho(h)$  density as function of depth
- ω storativity ratio, dimensionless

 $\lambda$  interporosity flow coefficient, dimensionless

- $\chi$  factor for apparent time =  $16/\pi^2$
- $\mu$  viscosity, cp

Subscripts

b bulk/breakdown pressure (fracture pressure)

- D dimensionless quantity
- f fracture
- H maximum horizontal
- h minimum horizontal
- i injected
- m matrix
- max maximum
- r reservoir
- R radial flow
- w wellbore
- x intersection point between radial flow and unit slope line at intermediate times/x axis
- y y axis
- z z axis
- 1 beginning of the trough
- 2 base of the trough
- 3 end of the trough

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